

b) tensor product of differential modules

M, N over C :

$$M \square_C N = \text{equalizer } M \otimes N \begin{array}{c} \xrightarrow{\Delta \otimes 1} \\ \xrightarrow{1 \otimes \Delta} \end{array} M \otimes C \otimes N$$

c) formal properties

assoc: $(Y \times_A Z) \times_B W = Y \times_A (Z \times_B W)$

unit: $(M \square_C N) \square_D P = M \square_C (N \square_D P)$

$$\begin{array}{ccc} Y \xrightarrow{\Delta} Y \times X & & Y \xrightarrow{\Delta} X \times Y \\ \parallel \searrow & \uparrow & \parallel \searrow \\ & Y \times X & \\ & \times & \\ & X \times Y & \end{array}$$

$$\begin{array}{ccc} M \xrightarrow{\Delta} M \otimes C & & M \xrightarrow{\Delta} C \otimes M \\ \parallel \searrow & \uparrow & \parallel \searrow \\ & M \square_C C & \\ & & \\ & & C \square_C M \end{array}$$

d) connection map

$$\eta: C(E) \xrightarrow{(X)} C(Y) \square C(Z) \subseteq C(Y) \otimes C(Z)$$

$(h \otimes k) \Delta$

i.e. $\eta: E = Y \times_X Z \rightarrow Y \square_X Z$