

$$i) \quad d(x \otimes 1) = dx \otimes 1 \quad (\Leftrightarrow F \text{ is a subcomplex})$$

$$ii) \quad d(x \otimes c) = dx \otimes c + (-1)^{\deg x} x \otimes dc + \tau(x \otimes c) \otimes 1$$

$$+ \sum \tau(x \otimes c') \otimes c''$$

$$\text{where } c \in \bar{C}, \quad \bar{\Delta}(c) = \sum c' \otimes c''$$

( $\Leftrightarrow E$  is a diff comodule)

$$iii) \quad d\tau(x \otimes c) + \tau(dx \otimes c) + (-1)^{\deg x} \tau(x \otimes dc) + \sum \tau[\tau(x \otimes c') \otimes c''] = 0$$

$$(\Leftrightarrow d^2 = 0)$$

Proper injective resolutions:

a)  $f: M \rightarrow N$  is a proper mono. of comodules:

a1)  $f$  is a morphism of diff comodules

a2)  $f$  is an  $R$ -split mono. of chain complexes

b)  $M$  is a proper injective:

$$M = V \otimes C \quad (\text{or a retract thereof})$$

$$c) \quad \text{coker}(f: M \rightarrow N) = M / \text{image } f$$

Can make proper injective resolutions

$$0 \rightarrow M \rightarrow Q_+ \text{ as follows:}$$